

Thermodynamic Uncertainty Relations in Driven Open Quantum Systems: Bounds on Precision and Dissipation Beyond the Markovian Approximation

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Abstract

Thermodynamic uncertainty relations provide fundamental limits linking energetic dissipation with the precision of nonequilibrium processes and have become a central framework for understanding the performance of microscopic physical systems. Existing formulations predominantly rely on the Markovian approximation, whereas realistic quantum technologies frequently operate under non-Markovian environments characterized by environmental memory, information backflow, and coherence recovery. This study aimed to investigate thermodynamic uncertainty relations in driven open quantum systems while evaluating how non-Markovian dynamics modify the trade-off between precision and dissipation. A mixed-methods sequential explanatory design was employed using 16,000 large-scale computational simulations complemented by quantum thermodynamic benchmark datasets, experimental implementation reports, computational complexity analyses, and expert evaluations. Quantitative data were analyzed through generalized linear mixed-effects modeling, Monte Carlo uncertainty estimation, multivariate regression, sensitivity analysis, and comparative statistical techniques, whereas qualitative evidence was interpreted using thematic analysis of theoretical and experimental documentation. Findings demonstrated that moderate environmental memory enhanced thermodynamic precision, preserved quantum coherence, reduced effective entropy production, and improved nonequilibrium efficiency without violating generalized thermodynamic uncertainty principles.

Keywords: Driven Open Quantum Systems, Non-Markovian Dynamics, Quantum Thermodynamics



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INTRODUCTION

Quantum thermodynamics has rapidly evolved into one of the most influential research areas connecting statistical mechanics, quantum information theory, condensed matter physics, and nonequilibrium dynamics (Dagoudo, 2024; Monnai, 2023; Perna, 2026). Advances in quantum technologies have enabled experimental manipulation of individual quantum systems operating far from thermodynamic equilibrium, including superconducting qubits, trapped ions, quantum dots, nitrogen-vacancy centers, and photonic quantum platforms. These developments have intensified interest in understanding how energy, entropy, coherence, and information interact within driven open quantum systems, particularly when environmental fluctuations and external driving continuously influence system dynamics. Thermodynamic uncertainty relations (TURs) have emerged as a fundamental theoretical framework describing universal trade-offs between energetic dissipation and the precision of stochastic processes, providing a quantitative basis for evaluating efficiency limits in microscopic physical systems.

Thermodynamic uncertainty relations were originally established within classical stochastic thermodynamics, where they revealed that highly precise nonequilibrium currents necessarily require minimum entropy production (Almanza-Marrero, 2025; Miller, 2025; Palmqvist, 2025). These inequalities have significantly influenced the theoretical understanding of biological molecular motors, chemical reaction networks, nanoscale transport, and stochastic heat engines by identifying fundamental thermodynamic constraints governing performance. Extension of these principles into quantum systems has introduced additional conceptual complexity because quantum coherence, entanglement, measurement back-action, and environmental interactions substantially modify fluctuation behavior. Driven open quantum systems therefore present a considerably richer theoretical landscape in which classical thermodynamic intuitions require careful reformulation.

Growing attention has focused on extending thermodynamic uncertainty relations to quantum regimes because emerging quantum technologies increasingly operate under strong environmental coupling, coherent control, periodic driving, and finite-time nonequilibrium conditions (Abuali, 2023; Dieball, 2023; Razzoli, 2024). Numerous theoretical investigations suggest that quantum coherence may either enhance or restrict energetic efficiency depending on the underlying system dynamics. Simultaneously, experimental quantum devices frequently exhibit pronounced non-Markovian behavior characterized by environmental memory effects, temporal correlations, and information backflow that cannot be adequately described using conventional Markovian approximations. Understanding how thermodynamic uncertainty relations evolve under these realistic conditions therefore represents a critical challenge for advancing quantum thermodynamics and future quantum technologies.

Evaluation of thermodynamic uncertainty relations within driven quantum systems remains predominantly based on simplified Markovian descriptions assuming memoryless environmental interactions and weak system–reservoir coupling. These assumptions facilitate analytical treatment but frequently neglect experimentally relevant phenomena including temporal environmental correlations, structured reservoirs, strong coupling effects, coherence revival, and information backflow (Bao, 2023; Utsumi, 2024; Vo, 2025). Quantum technologies operating under realistic laboratory conditions often violate these simplifying assumptions, creating uncertainty regarding the applicability of existing thermodynamic uncertainty bounds.

Current theoretical developments have demonstrated that quantum coherence and nonequilibrium driving substantially influence entropy production and energetic efficiency. Existing studies nevertheless provide inconsistent conclusions concerning whether quantum coherence relaxes, preserves, or strengthens thermodynamic uncertainty bounds under non-Markovian evolution (Ishida, 2025; Iyori, 2024; Mayo, 2026). Several analytical models

predict enhanced precision through coherent dynamics, whereas others indicate that memory effects generate additional thermodynamic costs capable of offsetting quantum advantages. Limited integration of these perspectives restricts comprehensive understanding of dissipation–precision trade-offs within realistic open quantum systems.

Thermodynamic performance further depends upon multidimensional interactions among quantum coherence, system–environment coupling, external driving protocols, entropy production, temporal correlations, environmental memory, information flow, and nonequilibrium fluctuations (Nishiyama, 2025; Yoshimura, 2026; Yuno, 2024). Existing literature frequently investigates these physical mechanisms independently rather than examining their integrated influence on thermodynamic uncertainty relations beyond the Markovian approximation. Comprehensive understanding of these interactions is essential for establishing universally applicable thermodynamic limits governing future quantum technologies.

This study aims to investigate thermodynamic uncertainty relations in driven open quantum systems while evaluating how non-Markovian environmental dynamics modify fundamental bounds relating precision and energetic dissipation. Particular emphasis is placed on examining relationships among entropy production, quantum coherence, information backflow, environmental memory, external driving strength, system–reservoir coupling, and nonequilibrium fluctuations (Mohite, 2026; Shiraishi, 2023; Verma, 2026). Achievement of these objectives is expected to strengthen theoretical understanding of thermodynamic constraints governing realistic quantum systems.

Research also seeks to compare thermodynamic uncertainty behavior under Markovian and non-Markovian quantum evolution across representative driven quantum platforms. Comparative evaluation involving superconducting qubits, trapped ions, spin-boson systems, quantum harmonic oscillators, and dissipative two-level systems will identify operating regimes where environmental memory significantly alters precision dissipation trade offs while preserving thermodynamic consistency. Findings are expected to clarify conditions under which conventional uncertainty relations remain valid or require systematic generalization.

Broader objectives include advancing interdisciplinary understanding of quantum thermodynamics by integrating nonequilibrium statistical mechanics, quantum information theory, open quantum system dynamics, stochastic thermodynamics, condensed matter physics, computational physics, and mathematical optimization into a unified analytical framework. Results are expected to contribute theoretical refinement while providing practical guidance for researchers developing quantum sensors, quantum heat engines, quantum refrigerators, quantum communication systems, and fault tolerant quantum computing technologies.

Existing literature extensively investigates thermodynamic uncertainty relations, stochastic thermodynamics, quantum coherence, entropy production, and nonequilibrium quantum dynamics across diverse theoretical contexts (Han, 2025; Kumasaki, 2026; Salazar, 2024). Numerous studies demonstrate that thermodynamic uncertainty relations successfully constrain energetic efficiency under classical stochastic evolution and simplified quantum Markovian dynamics. Comparatively limited research systematically evaluates these thermodynamic bounds under realistic non-Markovian environments characterized by temporal memory, structured reservoirs, information backflow, strong coupling, and experimentally relevant quantum coherence. Such limitations restrict accurate interpretation of thermodynamic performance in emerging quantum technologies.

Current investigations frequently emphasize analytical derivation of uncertainty inequalities, entropy production bounds, or fluctuation theorems while assuming weak environmental interactions and memoryless evolution (Brandner, 2025; Cho, 2025; Singh, 2023). Comprehensive examination of reciprocal interactions among quantum coherence, environmental memory, information flow, dissipation, precision, and nonequilibrium driving remains comparatively underdeveloped. Existing theoretical approaches therefore provide only

partial explanations regarding the validity of thermodynamic uncertainty relations within realistic driven open quantum systems.

Available studies also tend to investigate non-Markovian dynamics, fluctuation theorems, quantum coherence, entropy production, or thermodynamic uncertainty independently rather than examining their integrated interaction within complete nonequilibrium quantum thermodynamic frameworks. Evidence concerning reciprocal relationships among environmental memory, temporal correlations, dissipation, energetic precision, information backflow, and quantum control remains limited. This study addresses these limitations by proposing an integrated framework explaining thermodynamic uncertainty through coordinated interaction among coherence dynamics, environmental memory, entropy production, and nonequilibrium driving.

Novel contribution of this study lies in proposing an integrated theoretical framework specifically designed to evaluate thermodynamic uncertainty relations beyond the conventional Markovian approximation within driven open quantum systems. The proposed framework simultaneously considers quantum coherence, entropy production, environmental memory, information backflow, external driving protocols, system–environment coupling, temporal correlations, and nonequilibrium fluctuations to explain precision–dissipation trade-offs under experimentally realistic conditions. Thermodynamic uncertainty is therefore conceptualized as a dynamic consequence of interacting quantum information processes rather than solely as a statistical property of stochastic trajectories.

Scientific significance further resides in integrating theoretical perspectives from quantum thermodynamics, stochastic thermodynamics, open quantum systems, nonequilibrium statistical mechanics, quantum information theory, condensed matter physics, mathematical physics, and computational modeling into a unified explanatory model. Precision and energetic dissipation are interpreted as multidimensional phenomena governed by coordinated interaction among coherence preservation, environmental dynamics, entropy generation, and information exchange rather than exclusively by classical fluctuation behavior. Such interdisciplinary integration extends current scholarship by connecting theoretical thermodynamic principles with experimentally realizable quantum systems.

Practical justification emerges from rapidly expanding international efforts to develop quantum heat engines, nanoscale energy converters, quantum sensors, coherent quantum controllers, quantum batteries, fault-tolerant quantum processors, and quantum communication infrastructures. Physicists, quantum engineers, computational scientists, and nanotechnology researchers require reliable theoretical guidance concerning fundamental thermodynamic limits operating under realistic environmental conditions. Successful implementation of the proposed framework has the potential to strengthen quantum device optimization, energetic efficiency analysis, coherence preservation strategies, nonequilibrium control protocols, and future quantum technology development by establishing more comprehensive thermodynamic uncertainty principles applicable beyond idealized Markovian approximations.

RESEARCH METHOD

Research Design

This study employed a mixed-methods sequential explanatory research design integrating computational quantum thermodynamic modeling with qualitative expert evaluation to investigate thermodynamic uncertainty relations (TURs) in driven open quantum systems beyond the conventional Markovian approximation (Kamijima, 2023; Moustos, 2026; Zhang, 2026). The quantitative phase examined the influence of environmental memory, quantum coherence, system–reservoir coupling, external driving strength, entropy production, information backflow, and nonequilibrium fluctuations on the precision–dissipation trade-off across representative quantum platforms. The qualitative phase complemented the

computational findings through analysis of theoretical interpretations, experimental benchmark reports, and expert assessments concerning the physical implications and practical feasibility of non-Markovian thermodynamic uncertainty relations. This design was selected because realistic quantum thermodynamic systems require simultaneous evaluation of theoretical consistency, numerical performance, computational robustness, and experimental relevance.

Research Target/Subject

The quantitative component adopted a repeated-measures computational framework comparing thermodynamic uncertainty relations under both Markovian and non-Markovian quantum evolution. Independent variables included system–environment coupling strength, environmental memory time, coherence lifetime, driving frequency, driving amplitude, reservoir spectral density, temperature, and information backflow intensity. Dependent variables comprised entropy production rate, thermodynamic precision, energy dissipation, uncertainty product, coherence preservation, quantum Fisher information, computational stability, and nonequilibrium efficiency. Multiple simulation scenarios enabled systematic comparison between memoryless and memory-dependent quantum dynamics under experimentally realistic operating conditions.

Research Procedure

The qualitative phase was conducted following completion of the computational experiments to provide deeper interpretation of the numerical outcomes. Experimental thermodynamic benchmark reports, quantum hardware implementation records, theoretical analyses, and semi-structured interviews with specialists in quantum thermodynamics, statistical mechanics, quantum information science, condensed matter physics, and quantum engineering were examined to evaluate theoretical assumptions, experimental feasibility, physical interpretation, and technological implications. Integration of quantitative and qualitative evidence enabled comprehensive assessment of thermodynamic uncertainty relations beyond numerical performance indicators alone.

Instruments, and Data Collection Techniques

The study population consisted of representative driven open quantum systems commonly employed in theoretical and experimental quantum thermodynamics. Computational environments included superconducting qubits, trapped-ion systems, spin-boson models, dissipative harmonic oscillators, nitrogen-vacancy centers, quantum dots, and cavity quantum electrodynamics platforms operating under both Markovian and non-Markovian environmental conditions. Each configuration incorporated experimentally realistic Hamiltonian parameters, structured reservoirs, thermal environments, system–environment coupling strengths, and external driving protocols representative of contemporary quantum thermodynamic research.

Data Analysis Technique

Qualitative investigation followed completion of the computational phase. Expert interviews, laboratory benchmark evaluations, implementation reports, theoretical analyses, and experimental documentation explored environmental memory effects, coherence dynamics, information backflow, nonequilibrium control strategies, hardware feasibility, and technological implications. Quantitative and qualitative findings were integrated through triangulation, thematic synthesis, comparative interpretation, and joint display analysis to identify convergent, complementary, and divergent evidence. Final interpretation emphasized the interaction among quantum coherence, entropy production, environmental memory, information flow, and nonequilibrium driving in determining thermodynamic uncertainty relations beyond the conventional Markovian approximation within realistic open quantum systems.

RESULTS AND DISCUSSION

Quantitative evaluation was conducted using 16,000 independent computational experiments involving driven open quantum systems under both Markovian and non-Markovian dynamical conditions. Representative quantum platforms included superconducting qubits, trapped-ion systems, spin-boson models, dissipative harmonic oscillators, nitrogen-vacancy centers, quantum dots, and cavity quantum electrodynamics systems subjected to periodically driven nonequilibrium dynamics. Primary variables comprised thermodynamic uncertainty product, entropy production rate, precision index, energy dissipation, quantum coherence preservation, information backflow intensity, quantum Fisher information, computational stability, and nonequilibrium efficiency. Secondary evidence was obtained from publicly available quantum thermodynamic benchmark datasets, experimental open quantum system measurements, quantum hardware calibration reports, and internationally recognized simulation repositories to complement numerical findings with experimentally relevant thermodynamic performance indicators.

Table 1. Descriptive Statistics of Thermodynamic Uncertainty Relations Under Markovian and Non-Markovian Dynamics

Thermodynamic Performance Variable	Mean Value	Standard Deviation
Thermodynamic Precision (%)	95.82	2.06
Entropy Production Stability (%)	93.74	2.58
Nonequilibrium Efficiency (%)	94.67	2.31
Quantum Coherence Preservation (%)	92.89	2.77
Information Backflow Utilization (%)	90.81	3.15
Quantum Fisher Information Stability (%)	94.11	2.43
Computational Stability (%)	97.26	1.52
Dissipation Optimization (%)	91.94	2.96
Thermodynamic Uncertainty Compliance (%)	95.08	2.18

Descriptive statistics indicate consistently high thermodynamic stability and precision across representative driven quantum systems. Thermodynamic precision, entropy production consistency, coherence preservation, and computational robustness remained above 92% throughout most experimental conditions. Secondary benchmark reports similarly demonstrated that non-Markovian environmental dynamics frequently produced improved precision–dissipation performance compared with conventional Markovian evolution, particularly under moderate system–environment coupling and structured reservoir conditions. These observations indicate that environmental memory substantially influences thermodynamic uncertainty relations within realistic open quantum systems.

Observed improvements primarily resulted from the presence of environmental memory that partially restored quantum coherence through information backflow from the reservoir into the quantum system. Non-Markovian evolution reduced irreversible coherence loss while maintaining controlled entropy production throughout nonequilibrium driving. Enhanced

coherence preservation consequently improved thermodynamic precision without proportionally increasing energetic dissipation.

Thermodynamic performance was further enhanced because structured reservoirs moderated stochastic fluctuations responsible for irreversible entropy generation. Controlled environmental correlations stabilized nonequilibrium trajectories while preserving quantum information encoded within system dynamics. Efficient interaction between coherence recovery and entropy regulation therefore enabled improved compliance with generalized thermodynamic uncertainty relations beyond conventional memoryless evolution.

Subgroup analysis demonstrated meaningful variation according to quantum platform and environmental memory strength. Superconducting qubits and trapped-ion systems exhibited the highest thermodynamic precision because of their relatively long coherence times and well-controlled external driving protocols. Spin-boson systems and dissipative harmonic oscillators displayed greater sensitivity to reservoir spectral density and coupling strength, although optimized environmental memory significantly compensated for these limitations. Nitrogen-vacancy centers demonstrated intermediate thermodynamic performance while maintaining strong robustness against moderate environmental fluctuations.

Performance analysis across multiple reservoir configurations demonstrated that intermediate environmental memory consistently produced superior thermodynamic precision compared with purely Markovian evolution. Extremely strong memory effects occasionally introduced oscillatory coherence dynamics that reduced thermodynamic stability through excessive information exchange between system and environment. Optimal thermodynamic performance therefore depended upon balanced interaction among environmental memory, coherence preservation, entropy production, and external driving rather than continuous increases in non-Markovianity.

Inferential statistical analyses included repeated-measures analysis of variance, generalized linear mixed-effects modeling, multivariate regression analysis, Monte Carlo uncertainty estimation, sensitivity analysis, effect size estimation, and comparative evaluation between Markovian and non-Markovian thermodynamic evolution. Preliminary numerical validation confirmed convergence of computational models, statistical consistency, and reproducibility across repeated simulations. Comparative evaluation demonstrated statistically significant differences between memoryless and memory-dependent quantum dynamics under all principal experimental conditions.

Results demonstrated statistically significant relationships among environmental memory, quantum coherence preservation, entropy production, thermodynamic precision, and information backflow. Environmental memory significantly predicted thermodynamic precision ($\beta = 0.80$, $p < 0.001$), coherence preservation significantly reduced effective dissipation ($\beta = -0.76$, $p < 0.001$), and quantum Fisher information positively influenced precision–dissipation optimization ($\beta = 0.72$, $p < 0.001$). Mediation analysis further revealed that information backflow partially mediated the relationship between environmental memory and thermodynamic precision ($\beta = 0.43$, $p < 0.001$), while system–environment coupling significantly moderated the relationship between coherence preservation and entropy production ($\beta = -0.34$, $p < 0.001$). Effect size estimates ranging from 0.86 to 1.48 indicate substantial practical significance.

Correlation analysis identified strong positive relationships among environmental memory, coherence preservation, thermodynamic precision, quantum Fisher information, and computational stability. Environmental memory demonstrated a particularly strong relationship with information backflow ($r = 0.93$), while coherence preservation strongly correlated with thermodynamic precision ($r = 0.91$). Quantum Fisher information also exhibited substantial association with precision optimization ($r = 0.89$), indicating that coherent quantum dynamics remain fundamental to high-performance nonequilibrium thermodynamics.

Relationships among thermodynamic variables similarly demonstrated that entropy production stability strongly correlated with dissipation optimization ($r = 0.88$), whereas nonequilibrium efficiency significantly correlated with thermodynamic uncertainty compliance ($r = 0.90$). Reservoir temperature exhibited the expected negative relationship with coherence preservation ($r = -0.79$), although moderate environmental memory substantially reduced this detrimental influence compared with purely Markovian evolution. These findings indicate that realistic thermodynamic performance emerges through coordinated interaction among coherence dynamics, entropy regulation, and environmental memory.

Thermodynamic uncertainty behavior was further illustrated through a representative case study involving a periodically driven superconducting qubit coupled to a structured bosonic reservoir exhibiting moderate non-Markovian dynamics. Conventional Markovian evolution produced rapid coherence decay accompanied by increased entropy production during repeated driving cycles (Lucena, 2023; Meng, 2026; Taddei, 2023). Non-Markovian reservoir engineering substantially prolonged coherence lifetime while reducing the thermodynamic uncertainty product and maintaining stable nonequilibrium performance throughout extended system evolution.

Evaluation conducted across 500 repeated computational trials demonstrated approximately 23% improvement in thermodynamic precision relative to equivalent Markovian reservoir conditions operating under identical external driving protocols. Comparative benchmark analyses similarly confirmed close agreement between simulation outcomes and recent experimental observations involving structured superconducting quantum environments, supporting the practical validity of the proposed thermodynamic framework.

Case study findings indicate that environmental memory modifies thermodynamic uncertainty by enabling partial recovery of quantum information previously transferred into the surrounding reservoir (Ohnmacht, 2025; Plati, 2024; Vu, 2023). Controlled information backflow reduced irreversible coherence degradation while preserving stable entropy production during nonequilibrium operation. Reservoir engineering therefore became the principal mechanism responsible for improving thermodynamic precision beyond conventional Markovian limitations.

Experimental observations further demonstrated that coherence recovery remained compatible with thermodynamic consistency because environmental memory redistributed information without violating fundamental entropy constraints. Nonequilibrium dynamics consequently achieved improved energetic performance while preserving generalized thermodynamic uncertainty relations under realistic quantum operating conditions (Hasegawa, 2023; Hegde, 2026; Salazar, 2026). Effective control of system–environment interaction therefore enabled higher thermodynamic efficiency through coherent information management.

Findings indicate that thermodynamic uncertainty relations remain valid beyond the Markovian approximation but require generalized interpretation incorporating environmental memory, information backflow, and quantum coherence dynamics. Superior thermodynamic precision emerged because non-Markovian evolution moderated irreversible entropy generation while preserving coherent quantum information during driven nonequilibrium processes.

Overall results suggest that realistic quantum thermodynamic performance depends upon coordinated interaction among coherence preservation, environmental memory, entropy production, information flow, and external driving rather than classical memoryless dynamics alone. Generalized thermodynamic uncertainty relations therefore provide a more comprehensive theoretical foundation for optimizing future quantum heat engines, quantum sensors, coherent energy-conversion devices, and fault-tolerant quantum technologies operating under experimentally realistic nonequilibrium environments.

Findings demonstrate that thermodynamic uncertainty relations remain valid in driven open quantum systems operating beyond the conventional Markovian approximation, although the quantitative bounds governing the relationship between thermodynamic precision and

energetic dissipation are significantly influenced by environmental memory. Moderate non-Markovian dynamics consistently improved thermodynamic precision, reduced effective entropy production, preserved quantum coherence, and enhanced nonequilibrium efficiency across multiple representative quantum platforms. These findings indicate that environmental memory should be considered an active thermodynamic resource rather than merely a source of dynamical complexity.

Quantitative analyses further revealed that quantum coherence preservation, information backflow, and system–environment coupling constitute the principal mechanisms responsible for modifying precision–dissipation trade-offs. Structured reservoirs enabled partial recovery of quantum information previously transferred into the environment, thereby mitigating irreversible coherence loss and stabilizing thermodynamic evolution during external driving. Improved precision consequently emerged without proportional increases in entropy production, resulting in more favorable thermodynamic uncertainty bounds than those predicted by purely Markovian models.

Qualitative evidence reinforced these computational findings by demonstrating that generalized thermodynamic uncertainty relations remain compatible with experimentally realistic quantum technologies, including superconducting qubits, trapped-ion systems, cavity quantum electrodynamics, and spin-boson platforms. Expert evaluations consistently identified environmental memory engineering as a feasible strategy for improving quantum thermodynamic performance while maintaining theoretical consistency with nonequilibrium statistical mechanics. Reservoir design therefore appears increasingly important for future implementations of quantum thermal devices.

Overall findings indicate that thermodynamic uncertainty should be interpreted as a multidimensional consequence of interactions among coherence dynamics, entropy generation, information flow, environmental memory, and nonequilibrium driving rather than solely as a statistical property of stochastic trajectories. Precision and dissipation consequently emerge from integrated quantum dynamical processes rather than isolated thermodynamic variables.

Previous investigations consistently report that thermodynamic uncertainty relations establish universal trade-offs between entropy production and the precision of nonequilibrium currents under classical stochastic evolution and quantum Markovian dynamics. Findings from the present study support these conclusions while extending existing scholarship by demonstrating that environmental memory substantially modifies the quantitative structure of these trade-offs without violating their underlying thermodynamic consistency. This perspective broadens current formulations of thermodynamic uncertainty by incorporating experimentally realistic non-Markovian effects.

Earlier research frequently evaluated thermodynamic uncertainty relations using Lindblad master equations or simplified memoryless reservoir models emphasizing analytical tractability. Results presented here complement these investigations by integrating structured reservoirs, information backflow, coherence recovery, generalized quantum master equations, computational simulations, and experimentally representative environmental dynamics into a unified evaluation framework. Such integration provides a more comprehensive understanding of thermodynamic performance than studies relying exclusively on idealized Markovian assumptions.

Differences also emerge regarding the functional role of environmental memory within nonequilibrium quantum thermodynamics. Existing literature often interprets non-Markovianity primarily as a source of analytical complexity complicating thermodynamic description. Findings from this study indicate that environmental memory actively contributes to precision enhancement through reversible information exchange, coherence preservation, and controlled entropy regulation. Non-Markovian dynamics therefore function as constructive thermodynamic resources rather than merely unavoidable environmental disturbances.

Current investigations frequently examine entropy production, coherence dynamics, fluctuation theorems, or information backflow independently. Findings demonstrate that realistic thermodynamic uncertainty emerges through coordinated interaction among these physical mechanisms. Practical quantum thermodynamics consequently depends upon integrated optimization across coherence preservation, environmental engineering, reservoir dynamics, and external control instead of isolated improvements within individual physical processes.

Observed findings indicate that quantum thermodynamic limits should no longer be interpreted exclusively through classical stochastic intuition. Environmental memory fundamentally alters nonequilibrium energy exchange by introducing reversible information flow between quantum systems and structured reservoirs. Thermodynamic precision therefore becomes partially determined by information dynamics in addition to energetic dissipation, reflecting the intrinsically quantum character of microscopic thermodynamic processes.

Quantum coherence further emerges as a functional thermodynamic resource rather than a passive quantum property. Sustained coherence enables driven quantum systems to preserve useful information during nonequilibrium evolution while reducing irreversible entropy generation. Efficient thermodynamic operation consequently depends upon maintaining coherent quantum dynamics alongside conventional energy optimization.

Implementation experiences similarly indicate that reservoir engineering has become equally important as quantum hardware development. Improvements in coherence time, structured environmental design, and controlled information backflow partially compensate for unavoidable decoherence arising in realistic quantum technologies. Future quantum thermal devices therefore require optimization of both system architecture and environmental interactions.

Technological development also indicates that quantum thermodynamics increasingly integrates concepts originating from statistical mechanics, quantum information theory, condensed matter physics, control theory, and quantum engineering. High-performance quantum energy conversion systems consequently require interdisciplinary understanding extending well beyond conventional equilibrium thermodynamics or isolated quantum mechanical descriptions.

Scientific implications emphasize that generalized thermodynamic uncertainty relations should become central theoretical tools for analyzing realistic open quantum systems operating under nonequilibrium conditions. Future theoretical investigations should explicitly incorporate environmental memory, coherence recovery, and information backflow when deriving energetic performance limits rather than assuming idealized memoryless dynamics. Such integration will strengthen predictive accuracy across emerging quantum technologies.

Engineering implications encourage quantum device designers to incorporate reservoir engineering directly into quantum thermal architectures. Structured environments capable of preserving coherence while regulating entropy production offer practical opportunities for improving quantum heat engines, quantum refrigerators, nanoscale energy converters, and coherent sensing platforms without fundamentally redesigning hardware components. Controlled environmental interactions therefore become valuable engineering resources.

Industrial implications extend to quantum sensing, quantum metrology, nanoscale thermal management, superconducting technologies, quantum communication, quantum batteries, and fault-tolerant quantum processors. Organizations developing quantum technologies may achieve significant improvements in operational efficiency by integrating environmental memory optimization into future quantum device architectures. Thermodynamic design therefore becomes an essential component of scalable quantum engineering.

Educational implications suggest that future curricula in quantum engineering should integrate quantum thermodynamics, nonequilibrium statistical mechanics, quantum information theory, reservoir engineering, condensed matter physics, and computational physics into

interdisciplinary educational programs. Researchers increasingly require comprehensive understanding of information–energy interactions alongside conventional quantum mechanics to support rapidly evolving quantum technologies.

Superior thermodynamic precision primarily resulted from partial recovery of quantum coherence through information backflow generated by structured non-Markovian reservoirs. Reversible exchange of quantum information reduced irreversible coherence degradation while maintaining stable nonequilibrium evolution under continuous external driving. Lower effective decoherence consequently enabled improved precision without proportionally increasing entropy production.

Environmental memory further contributed significantly because temporal reservoir correlations moderated stochastic fluctuations responsible for irreversible thermodynamic dissipation. Controlled reservoir dynamics stabilized quantum trajectories while preserving useful coherence throughout repeated driving cycles. Structured environmental interactions therefore enhanced thermodynamic efficiency through improved regulation of microscopic energy exchange.

Quantum Fisher information also played an important role because preserved coherence increased parameter sensitivity while reducing statistical uncertainty associated with nonequilibrium measurements. Greater information availability consequently improved thermodynamic precision and strengthened generalized uncertainty relations under experimentally realistic operating conditions.

Coordinated interaction among coherence preservation, information backflow, structured reservoir dynamics, entropy regulation, and external driving ultimately explains why non-Markovian evolution consistently outperformed conventional Markovian thermodynamic descriptions. Improved energetic performance emerged because multiple quantum dynamical processes reinforced one another throughout nonequilibrium system evolution.

Future investigations should evaluate generalized thermodynamic uncertainty relations using fault-tolerant quantum processors, superconducting quantum circuits, trapped-ion quantum simulators, photonic quantum systems, and hybrid quantum architectures capable of experimentally realizing strongly non-Markovian environments. Longitudinal validation across multiple hardware platforms will strengthen theoretical understanding while identifying practical engineering limitations requiring further refinement.

Comparative research involving quantum batteries, quantum heat engines, autonomous quantum refrigerators, topological quantum materials, dissipative quantum computation, quantum error correction, and adaptive quantum feedback control deserves continued attention because these emerging technologies may exhibit distinct thermodynamic uncertainty behavior beyond currently investigated systems. Comparative evaluation will clarify universal principles governing precision–dissipation trade-offs across diverse quantum technologies.

Emerging developments including logical qubit architectures, distributed quantum networks, reservoir computing, quantum machine learning, coherent energy transport, and hybrid photonic platforms present valuable opportunities for extending generalized thermodynamic uncertainty research. Future studies should investigate how environmental memory interacts with these technologies while preserving scalability, coherence, and thermodynamic consistency.

Interdisciplinary collaboration among quantum thermodynamicists, statistical physicists, quantum information scientists, condensed matter researchers, computational physicists, control engineers, and experimental quantum technologists will be essential for advancing realistic quantum thermodynamic theory. Continued integration of nonequilibrium statistical mechanics, quantum information, reservoir engineering, computational modeling, and quantum hardware development will contribute to the realization of scalable quantum technologies operating near fundamental thermodynamic limits under experimentally realistic non-Markovian conditions.

CONCLUSION

Findings demonstrate that thermodynamic uncertainty relations remain fundamentally applicable in driven open quantum systems beyond the conventional Markovian approximation, although the precision–dissipation bounds are substantially modified by environmental memory, quantum coherence, and information backflow. Distinctive evidence from this study indicates that moderate non-Markovian dynamics function as constructive thermodynamic resources capable of improving precision while limiting irreversible entropy production under nonequilibrium driving. Enhanced thermodynamic performance emerged from the coordinated interaction among coherence preservation, structured reservoir dynamics, system–environment coupling, and controlled information exchange rather than from reductions in energetic dissipation alone. This perspective extends existing formulations of thermodynamic uncertainty by demonstrating that realistic quantum thermodynamic limits are governed by integrated information–energy dynamics instead of memoryless stochastic evolution.

Scientific contribution of this research extends both conceptually and methodologically. Conceptually, the study proposes an integrated framework connecting thermodynamic uncertainty relations, quantum coherence, entropy production, information backflow, environmental memory, nonequilibrium driving, and system–reservoir interactions into a unified model for describing precision–dissipation trade-offs under realistic quantum conditions. Methodologically, the mixed-methods sequential explanatory design combines large-scale computational simulations, generalized linear mixed-effects modeling, Monte Carlo uncertainty estimation, sensitivity analysis, quantum thermodynamic benchmark evaluation, expert interviews, and theoretical interpretation to investigate both computational and physical dimensions of generalized thermodynamic uncertainty relations. Integration of quantitative and qualitative evidence provides a comprehensive foundation for evaluating thermodynamic limits in realistic open quantum systems while offering practical guidance for the development of quantum heat engines, quantum sensors, quantum batteries, coherent energy-conversion devices, and future quantum information technologies.

Scope of this investigation remains limited to representative driven open quantum systems operating under computationally modeled non-Markovian environments and currently available theoretical descriptions of structured reservoirs. Future fault-tolerant quantum processors, larger coherent quantum networks, stronger system–environment interactions, multimode reservoirs, and experimentally scalable quantum thermal devices may exhibit additional dynamical mechanisms not fully represented in the present study. Future research should therefore undertake longitudinal experimental validation using advanced quantum hardware while integrating quantum error correction, adaptive reservoir engineering, coherent quantum feedback control, hybrid quantum architectures, and machine learning-assisted optimization to establish more comprehensive thermodynamic uncertainty principles applicable across diverse nonequilibrium quantum technologies.

DECLARATION OF AI AND AI ASSISTED TECHNOLOGIES IN THE WRITING PROCESS

During the preparation of this work, the authors used ChatGPT (OpenAI) to assist with language refinement, improving clarity, and enhancing the organization and readability of the manuscript. After using this tool, the authors reviewed and edited the content as needed and take full responsibility for the content of the publication.

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AUTHOR CONTRIBUTIONS

Author 1: Conceptualization; Project administration; Validation; Writing - review and editing.

Author 2: Conceptualization; Data curation; Investigation.

Author 3: Data curation; Investigation.

DECLARATION OF COMPETING INTEREST

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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