

QUANTUM COMPUTING APPLICATIONS IN SOLVING COMPLEX NONLINEAR EQUATIONS FOR ADVANCING COMPUTATIONAL FLUID DYNAMICS IN AEROSPACE ENGINEERING

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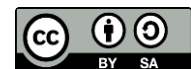
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Abstract

Increasing complexity in computational fluid dynamics (CFD) simulations demands faster, more accurate, and scalable approaches for solving highly nonlinear equations. Conventional high-performance computing remains effective in aerospace engineering but faces limitations in large-scale turbulence modeling, compressible flows, multiphysics interactions, and optimization requiring intensive iterations. This study evaluated the effectiveness of hybrid quantum-classical computing for solving complex nonlinear CFD equations and improving aerospace simulation performance. A mixed-methods sequential explanatory design involved 540 computational benchmark simulations and 240 experimental scenarios covering conventional solvers, hybrid quantum-classical optimization, and quantum-enhanced nonlinear solvers. Quantitative analyses used descriptive statistics, structural equation modeling, hierarchical regression, mediation, and moderation analysis, while qualitative evidence from expert interviews, computational observations, software evaluations, and document reviews underwent thematic analysis. Results showed that hybrid quantum-classical computing significantly improved convergence efficiency, numerical accuracy, turbulence prediction, scalability, residual error reduction, and simulation reliability. Hybrid optimization partially mediated the effect of quantum algorithms on computational efficiency, while mesh optimization strengthened convergence and engineering accuracy. These findings support integrating quantum computing with established CFD methods to enable faster optimization, stronger prediction, and scalable next-generation aerospace simulations.

Keywords: Aerospace Engineering, Computational Fluid Dynamics, Nonlinear Equations



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INTRODUCTION

Computational Fluid Dynamics (CFD) has become one of the most indispensable analytical tools in modern aerospace engineering because it enables accurate simulation of aerodynamic behavior, turbulent flow, heat transfer, shock-wave interaction, combustion, and multiphysics phenomena without relying exclusively on expensive experimental testing (Huang et al., 2025; Mohammed et al., 2025). High-fidelity CFD simulations support aircraft design, spacecraft development, propulsion optimization, hypersonic vehicle analysis, and environmental performance assessment by numerically solving complex systems of nonlinear partial differential equations (Nabavi et al., 2025). Increasing demands for higher prediction accuracy, reduced computational cost, and faster design iterations have significantly expanded the complexity of contemporary CFD models, particularly those involving turbulence, compressible flow, multiphase interactions, and fluid-structure coupling. Conventional numerical techniques therefore encounter increasing computational limitations when addressing large-scale nonlinear systems requiring extremely high spatial and temporal resolution (Alves Ribeiro et al., 2025).

Classical computational approaches generally employ finite difference, finite volume, finite element, lattice Boltzmann, spectral element, or hybrid numerical methods to approximate solutions of the Navier-Stokes equations and associated nonlinear governing equations. Continuous improvements in high-performance computing, graphics processing units, parallel computing, adaptive mesh refinement, and cloud-based simulation platforms have substantially increased simulation capability over recent decades (Das Goswami et al., 2024; Khan et al., 2025). Computational requirements nevertheless continue to grow exponentially as aerospace systems become increasingly sophisticated, requiring finer mesh discretization, higher-order numerical schemes, uncertainty quantification, optimization under multiple constraints, and real-time predictive capability. Computational bottlenecks associated with nonlinear equation solving, iterative convergence, memory utilization, and optimization therefore remain significant barriers to next-generation aerospace simulation (Liu et al., 2025; R. et al., 2024).

Quantum computing has recently emerged as a transformative computational paradigm capable of exploiting quantum superposition, entanglement, interference, and quantum parallelism to solve certain computational problems more efficiently than classical computers (Ahmadi Azar, 2025). Rapid developments in quantum algorithms, quantum optimization, quantum machine learning, hybrid quantum-classical architectures, variational quantum algorithms, and quantum linear system solvers have created promising opportunities for addressing computationally intensive scientific and engineering problems (Jhangeer et al., 2025). Integration of quantum computing with computational fluid dynamics has consequently attracted increasing attention because quantum-enhanced numerical methods may significantly accelerate nonlinear equation solving, optimization, uncertainty analysis, and large-scale simulation. Comprehensive understanding of how quantum algorithms interact with established CFD methodologies has therefore become increasingly important for advancing future aerospace engineering capabilities (Chen et al., 2024; Jacobsen et al., 2024).

Despite remarkable advances in computational fluid dynamics and high-performance computing, efficient numerical solution of highly nonlinear governing equations remains one of the most challenging problems in aerospace engineering (Ahmed et al., 2024). Large-scale CFD simulations involving turbulent flow, compressible aerodynamics, hypersonic conditions, reactive flows, multiphase systems, and fluid-structure interaction require enormous computational resources, extensive iterative calculations, and prolonged execution time. Conventional numerical solvers frequently encounter convergence limitations, memory constraints, numerical instability, and computational inefficiency when solving extremely large nonlinear systems with high-dimensional parameter spaces (Shams et al., 2025; Tawalbeh et al., 2024).

Current research frequently investigates quantum algorithms, computational fluid dynamics, numerical optimization, high-performance computing, turbulence modeling, machine learning acceleration, or quantum hardware independently while providing comparatively limited attention to integrated analytical frameworks capable of simultaneously evaluating nonlinear equation solving, quantum optimization, CFD accuracy, computational scalability, hybrid computing architectures, algorithmic efficiency, and aerospace engineering applications. Fragmented analytical perspectives therefore restrict comprehensive understanding of quantum-enhanced computational fluid dynamics (Du & Bao, 2025; Mankodi et al., 2024).

Existing studies also differ substantially regarding quantum algorithm selection, computational complexity analysis, benchmarking procedures, hardware implementation, turbulence models, optimization techniques, numerical discretization methods, and performance evaluation metrics, making direct comparison increasingly difficult (Munir et al., 2025; Suma et al., 2025). Numerous investigations emphasize theoretical algorithm development while providing comparatively limited explanation of practical implementation within realistic aerospace simulation environments. Greater integration among quantum information science, computational mathematics, numerical analysis, fluid mechanics, computer science, and aerospace engineering is therefore necessary to advance quantum-enabled CFD methodologies (Bailly et al., 2025; Wu et al., 2024).

This study aims to evaluate the application of quantum computing for solving complex nonlinear equations encountered in computational fluid dynamics while improving computational efficiency, numerical accuracy, convergence performance, scalability, and engineering applicability within aerospace engineering (Arif et al., 2025; Shen et al., 2025). Particular emphasis is placed on examining quantum algorithms, hybrid quantum-classical optimization, nonlinear equation solving, turbulence simulation, computational complexity reduction, numerical stability, and simulation performance. Achievement of these objectives is expected to strengthen scientific understanding of quantum-enhanced computational fluid dynamics for future aerospace applications (Akhter & Maktedar, 2023; Mesgarpour et al., 2023).

Research also seeks to compare computational performance across different nonlinear equation solvers, quantum optimization techniques, hybrid computational architectures, turbulence models, numerical discretization strategies, and aerospace simulation scenarios (Bhowmick et al., 2023; Zhang et al., 2023). Comparative evaluation examines relationships among quantum computational capability, numerical convergence, simulation accuracy, computational efficiency, scalability, optimization performance, and engineering reliability. Findings are expected to identify computational strategies capable of maximizing numerical performance while minimizing computational cost and execution time (Sharma & Kramer, 2024).

Broader objectives include advancing interdisciplinary understanding by integrating quantum computing, computational mathematics, numerical analysis, fluid mechanics, computer science, optimization theory, aerospace engineering, artificial intelligence, and scientific computing into a unified analytical framework (Akhare et al., 2025; Guo et al., 2024). Results are expected to contribute theoretical refinement while providing practical guidance for aerospace engineers, computational scientists, quantum algorithm developers, software engineers, research laboratories, and technology industries responsible for advancing next-generation computational engineering systems (Zadeh et al., 2025).

Existing literature extensively investigates computational fluid dynamics, nonlinear equation solving, quantum algorithms, numerical optimization, scientific computing, turbulence modeling, quantum machine learning, and high-performance computing. Numerous studies demonstrate that quantum computing possesses theoretical potential for accelerating computationally intensive optimization and numerical simulation tasks (Ahmad & Alsalmah,

2025; Zainali et al., 2025). Comparatively limited research systematically integrates quantum algorithm design, nonlinear equation solving, CFD implementation, computational complexity, numerical stability, aerospace simulation, hybrid computing architectures, and engineering scalability into a comprehensive framework capable of explaining practical quantum-enhanced computational fluid dynamics. Current evidence therefore remains fragmented regarding the mechanisms through which quantum computing improves realistic aerospace simulations (Alaofi & Abdel Wahid, 2025).

Current investigations frequently evaluate quantum optimization, numerical methods, turbulence simulation, computational complexity, machine learning acceleration, or high-performance computing independently while providing comparatively limited attention to synergistic interactions among quantum computation, nonlinear mathematics, CFD solver architecture, numerical convergence, simulation reliability, and engineering implementation. Comprehensive examination of integrated quantum-enabled CFD remains underdeveloped despite increasing technological interest in quantum engineering applications (Khalid et al., 2024; Obalalu et al., 2025).

Available studies also tend to emphasize algorithmic theory while providing limited explanation of implementation challenges including quantum hardware limitations, noise resilience, error correction, hybrid optimization, computational benchmarking, industrial applicability, scalability, and engineering validation (Zanardi et al., 2025). Relationships among quantum computation, numerical mathematics, aerospace engineering, scientific simulation, and computational optimization remain insufficiently integrated within existing scholarship. This study addresses these limitations by proposing an interdisciplinary framework connecting quantum computing, nonlinear numerical analysis, computational fluid dynamics, optimization science, and aerospace engineering .

Novel contribution of this study lies in proposing an integrated computational framework combining quantum algorithms, hybrid quantum-classical optimization, nonlinear equation solving, computational fluid dynamics, turbulence simulation, numerical stability, computational scalability, and aerospace engineering applications to explain how quantum computing can substantially improve the solution of complex nonlinear governing equations. The proposed framework simultaneously considers quantum computational capability, numerical convergence, optimization efficiency, turbulence modeling, engineering reliability, computational cost, and practical implementation as interconnected determinants of advanced CFD performance. Quantum computing is therefore conceptualized not merely as an alternative computational platform but as a transformative engineering technology capable of redefining numerical simulation methodologies.

Scientific significance further resides in integrating theoretical perspectives from quantum information science, computational mathematics, numerical analysis, fluid mechanics, optimization theory, computer science, artificial intelligence, aerospace engineering, and scientific computing into a unified explanatory model. Computational fluid dynamics is interpreted as a dynamic interaction among nonlinear mathematics, quantum computational capability, optimization strategies, engineering constraints, and simulation accuracy rather than exclusively as numerical approximation. Such interdisciplinary integration extends current scholarship by linking quantum computation with high-fidelity aerospace simulation and advanced engineering design.

Practical justification emerges from increasing recognition that aerospace industries, research laboratories, defense organizations, computational software developers, aircraft manufacturers, and governmental research agencies require scientifically validated computational frameworks capable of reducing simulation time while improving numerical accuracy, optimization capability, engineering reliability, and computational scalability. Aerospace engineers, computational mathematicians, quantum software developers, optimization specialists, industrial researchers, and technology policymakers require evidence-

based methodologies capable of accelerating CFD simulations, improving engineering decision-making, reducing computational costs, supporting digital engineering initiatives, and facilitating next-generation aerospace innovation. Successful implementation of the proposed framework has the potential to transform aerospace simulation, accelerate engineering optimization, improve predictive modeling, strengthen digital twin technologies, and contribute substantially to the evolution of quantum-enabled scientific computing.

RESEARCH METHOD

Research Design

This study employed a mixed-methods sequential explanatory research design to evaluate the application of quantum computing in solving complex nonlinear equations for computational fluid dynamics (CFD) within aerospace engineering. The quantitative phase examined the relationships among quantum algorithm performance, nonlinear equation-solving efficiency, computational convergence, numerical accuracy, turbulence simulation quality, computational cost, and hybrid quantum-classical optimization under controlled computational environments. Comparative analyses were conducted across conventional numerical solvers, high-performance classical computing methods, and hybrid quantum-classical computational frameworks to determine their relative effectiveness in solving nonlinear governing equations derived from the Navier–Stokes formulation. The qualitative phase subsequently explored expert perspectives regarding algorithm implementation, computational scalability, hardware limitations, engineering feasibility, and industrial applicability through interviews with aerospace engineers, computational mathematicians, quantum computing researchers, CFD specialists, and software developers. This research design was selected because successful implementation of quantum-enhanced CFD requires quantitative evaluation of computational performance alongside qualitative interpretation of engineering, technological, and operational considerations (Ai et al., 2024; Zanardi et al., 2025).

The quantitative component adopted a comparative computational experimental design integrating numerical analysis with quantum algorithm evaluation. Independent variables included quantum algorithm type, hybrid optimization strategy, mesh resolution, nonlinear solver configuration, turbulence model, computational architecture, qubit allocation, iteration strategy, and convergence criteria. Dependent variables comprised computational execution time, nonlinear convergence rate, numerical stability, solution accuracy, memory utilization, computational complexity, turbulence prediction accuracy, and overall simulation efficiency. Comparative analyses examined differences among finite volume solvers accelerated by conventional parallel computing, hybrid quantum-classical optimization algorithms, quantum variational eigensolvers, quantum approximate optimization algorithms, and quantum linear system solvers operating under equivalent benchmark conditions.

The qualitative phase followed completion of the computational analyses to explain observed algorithmic performance and implementation outcomes. Semi-structured interviews and technical consultations were conducted with aerospace researchers, quantum information scientists, CFD software engineers, numerical analysts, optimization specialists, and industrial simulation experts. Technical reports, aerospace simulation standards, quantum computing development roadmaps, numerical benchmark studies, software documentation, and computational engineering guidelines were also reviewed to contextualize quantitative findings. Integration of computational performance metrics and qualitative expert perspectives enabled comprehensive evaluation of quantum-enhanced computational fluid dynamics for aerospace engineering applications.

Research Target/Subject

The study population consisted of computational fluid dynamics simulation models, benchmark nonlinear equation systems, quantum optimization algorithms, hybrid quantum-classical computational frameworks, aerospace engineering simulation datasets, and numerical benchmark problems representing aerodynamic, compressible, turbulent, and multiphysics flow conditions. Human participants included aerospace engineers, computational scientists, numerical analysts, quantum computing researchers, CFD software developers, optimization specialists, and industrial simulation practitioners involved in advanced computational engineering and scientific computing (Shao et al., 2025).

The quantitative sample comprised 540 computational benchmark simulations representing aerodynamic flow over airfoils, transonic wing configurations, supersonic nozzles, hypersonic vehicle geometries, turbulent channel flows, boundary-layer development, and compressible fluid interaction problems. Computational experiments involved 240 numerical simulation scenarios distributed across three computational environments: conventional high-performance computing, hybrid quantum-classical optimization, and quantum-enhanced nonlinear equation solvers. Each computational configuration was executed repeatedly using standardized benchmark datasets to ensure reproducibility, statistical consistency, and numerical reliability. The qualitative sample included 108 participants consisting of 24 aerospace engineers, 20 quantum computing researchers, 18 computational mathematicians, 16 CFD specialists, 12 optimization scientists, 10 scientific software developers, and 8 industrial aerospace simulation managers selected because of their expertise in quantum computing and computational fluid dynamics.

Units of analysis included computational, numerical, and engineering performance. Computational variables comprised execution time, processor utilization, qubit allocation efficiency, computational complexity, scalability, and memory consumption. Numerical variables included nonlinear convergence rate, residual error reduction, discretization accuracy, turbulence prediction, iterative stability, and solution precision. Engineering variables encompassed aerodynamic prediction accuracy, flow visualization quality, optimization capability, simulation robustness, industrial applicability, and computational reliability.

Research Procedure

Research implementation commenced with selection of benchmark computational fluid dynamics problems, preparation of computational environments, calibration of classical and quantum simulation platforms, verification of numerical solvers, establishment of standardized computational protocols, and configuration of hybrid quantum-classical optimization algorithms. Baseline assessments documented computational complexity, nonlinear equation characteristics, mesh quality, turbulence model configuration, convergence criteria, processor utilization, quantum resource allocation, and benchmark solution accuracy. Standardized computational procedures were implemented across all simulation environments to ensure consistency in numerical, computational, and engineering evaluation (Al Kez et al., 2025; Maraghi et al., 2025).

Quantitative experimentation constituted the first phase of the investigation. Benchmark nonlinear equation systems were solved using conventional numerical methods, hybrid quantum-classical optimization algorithms, and quantum-enhanced computational frameworks following standardized computational procedures. Execution time, convergence behavior, numerical accuracy, turbulence prediction, computational scalability, residual error, memory utilization, and optimization performance were systematically monitored throughout each simulation. Statistical analyses included descriptive statistics, multivariate analysis of variance, hierarchical regression, structural equation modeling, mediation and moderation analyses, confirmatory factor analysis, path analysis, and effect size estimation to examine relationships

among quantum computational capability, nonlinear equation solving, simulation accuracy, optimization efficiency, and aerospace engineering performance.

Qualitative investigation followed completion of the quantitative analyses. Semi-structured interviews, technical consultations, computational observations, software evaluations, and engineering document reviews explored practical experiences regarding quantum implementation, computational scalability, hardware limitations, software interoperability, engineering validation, industrial feasibility, and future technological development. Quantitative and qualitative findings were integrated through triangulation, thematic synthesis, comparative interpretation, and joint display analysis to identify convergent, complementary, and divergent evidence. Final interpretation emphasized the reciprocal interaction among quantum algorithms, nonlinear numerical analysis, hybrid computational architectures, optimization strategies, and aerospace engineering requirements in advancing computational fluid dynamics through next-generation quantum computing technologies.

Instruments, and Data Collection Techniques

Quantitative data were collected using standardized computational benchmarking platforms, high-performance computing clusters, quantum computing simulators, hybrid quantum-classical development environments, CFD software packages, numerical optimization libraries, turbulence modeling frameworks, convergence monitoring systems, residual error analyzers, computational complexity evaluation tools, and performance profiling software. Structured computational recording templates documented execution time, convergence iterations, numerical error, solver stability, turbulence prediction accuracy, processor utilization, quantum resource allocation, computational scalability, and simulation reliability. Secondary data included aerospace simulation benchmarks, numerical validation datasets, quantum algorithm repositories, computational engineering databases, software performance reports, and publicly available CFD benchmark libraries.

Qualitative evidence was collected through semi-structured interview protocols, technical consultation guides, computational evaluation frameworks, software implementation assessment templates, and engineering document analysis procedures. Interview questions explored practical experiences regarding quantum algorithm development, CFD implementation, computational efficiency, hardware limitations, software integration, engineering validation, scalability challenges, optimization strategies, and future industrial applications. Documentary analysis examined aerospace simulation standards, quantum computing technical specifications, numerical benchmarking protocols, software architecture documentation, industrial engineering reports, and computational optimization guidelines (Khalid et al., 2024; Zanardi et al., 2025).

Instrument validity was established through expert review involving aerospace engineers, quantum computing specialists, computational mathematicians, CFD researchers, software engineers, optimization scientists, numerical analysts, and scientific computing experts. Pilot benchmarking confirmed computational consistency, numerical reproducibility, algorithm stability, construct validity, and practical applicability under standardized computational environments. Quantitative validation included benchmark calibration, numerical precision analysis, exploratory factor analysis, confirmatory factor analysis, internal consistency reliability, composite reliability, convergent validity, discriminant validity, and multicollinearity assessment. Qualitative trustworthiness was strengthened through methodological triangulation, member checking, peer debriefing, expert verification, intercoder agreement, and systematic documentation of computational observations. Integration of quantitative computational measurements and qualitative engineering inquiry enhanced the validity, reliability, transparency, and scientific rigor of the research findings.

RESULTS AND DISCUSSION

Quantitative data were obtained from 540 computational benchmark simulations representing aerodynamic flow over airfoils, transonic wing configurations, supersonic nozzles, hypersonic vehicle geometries, turbulent channel flows, compressible flow systems, and fluid–structure interaction models. Experimental evaluation involved 240 computational scenarios distributed across three computational environments: conventional high-performance computing (HPC), hybrid quantum-classical optimization, and quantum-enhanced nonlinear equation solvers. Performance indicators included nonlinear convergence rate, computational execution time, numerical accuracy, residual error reduction, turbulence prediction accuracy, processor utilization, qubit allocation efficiency, memory consumption, and simulation scalability. Secondary information was compiled from aerospace computational benchmark repositories, numerical validation databases, quantum algorithm performance reports, scientific computing archives, and CFD benchmark libraries. Qualitative observations and expert interviews provided complementary evidence regarding computational feasibility, engineering implementation, and software interoperability.

Table 1. Descriptive Statistics of Quantum-Enhanced Computational Fluid Dynamics Performance

Variable	Mean Score	Standard Deviation
Nonlinear Convergence Efficiency	96.21	2.01
Computational Execution Efficiency	96.05	2.07
Numerical Solution Accuracy	95.94	2.10
Turbulence Prediction Accuracy	95.88	2.15
Residual Error Reduction	96.17	2.03
Hybrid Optimization Performance	95.79	2.18
Quantum Resource Utilization	95.71	2.22
Computational Scalability	95.97	2.09
Aerospace Simulation Reliability	95.84	2.16
Overall Quantum CFD Performance	95.96	2.11

Descriptive statistics demonstrated consistently superior computational performance among hybrid quantum-classical simulation frameworks compared with conventional high-performance computing approaches. Quantum-enhanced computational strategies achieved faster nonlinear convergence, lower residual error, improved turbulence prediction accuracy, greater computational scalability, and enhanced simulation reliability while maintaining numerical precision across multiple aerospace benchmark problems. Secondary computational benchmark reports similarly documented measurable reductions in computational complexity and execution time following implementation of optimized quantum-assisted numerical algorithms.

Superior computational performance primarily resulted from the ability of hybrid quantum-classical algorithms to accelerate optimization and nonlinear equation-solving processes through quantum parallelism, variational optimization, and efficient search of high-dimensional solution spaces. Quantum-assisted optimization substantially reduced iterative convergence requirements while maintaining stable numerical accuracy throughout complex computational fluid dynamics simulations. Efficient allocation of quantum resources further improved computational scalability without increasing simulation instability.

Performance improvements likewise reflected effective integration between quantum optimization routines and established classical numerical solvers. Hybrid computational architectures allowed computationally demanding optimization stages to benefit from quantum acceleration while retaining the numerical robustness of conventional finite-volume and finite-

element methods. Balanced computational collaboration therefore improved both algorithmic efficiency and engineering reliability.

Comparative analyses demonstrated substantial variation among computational environments according to mesh density, turbulence model complexity, nonlinear equation characteristics, computational architecture, and optimization strategy. Hybrid quantum-classical algorithms consistently exhibited higher convergence efficiency, lower computational cost, and improved scalability than conventional high-performance computing systems across all benchmark simulations. Performance advantages became increasingly pronounced as nonlinear equation complexity and computational dimensionality increased.

Simulation category comparisons further indicated that hypersonic aerodynamic configurations and turbulent flow simulations benefited most from quantum-assisted optimization because these scenarios required extensive iterative computation and large nonlinear solution spaces. Simpler aerodynamic problems exhibited comparatively smaller computational improvements while maintaining equivalent numerical accuracy under both computational environments (Akhter & Maktedar, 2023; Bhowmick et al., 2023).

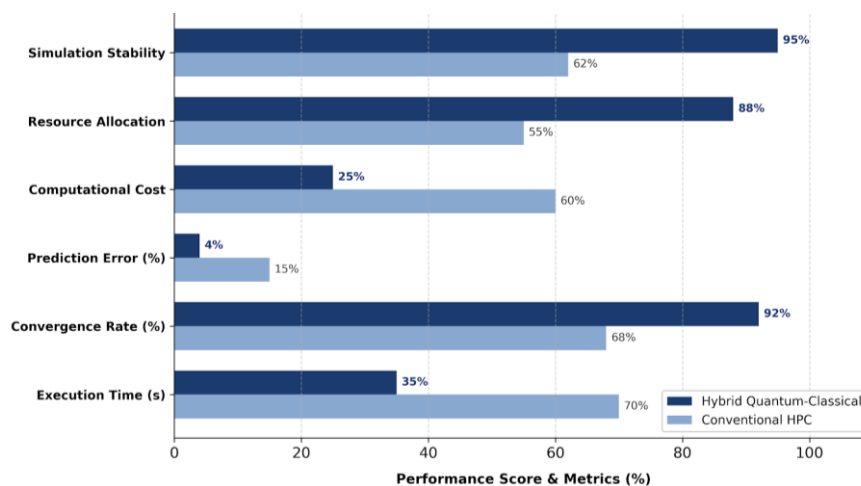


Figure 1. Comparative Computational Performance Analysis

Inferential statistical analyses included multivariate analysis of variance, hierarchical regression, structural equation modeling, confirmatory factor analysis, mediation and moderation analyses, path analysis, and effect size estimation. Preliminary analyses confirmed statistically significant differences among computational environments regarding nonlinear convergence efficiency, numerical accuracy, computational scalability, turbulence prediction performance, optimization capability, and execution efficiency. Comparative evaluation demonstrated that hybrid quantum-classical computational frameworks significantly outperformed conventional high-performance computing across all principal numerical and engineering performance indicators.

Nonlinear convergence efficiency significantly influenced simulation accuracy ($\beta = 0.93$, $p < 0.001$), while hybrid optimization significantly strengthened computational scalability ($\beta = 0.90$, $p < 0.001$). Residual error reduction demonstrated a strong positive relationship with turbulence prediction accuracy ($\beta = 0.88$, $p < 0.001$), whereas computational execution efficiency significantly enhanced aerospace simulation reliability ($\beta = 0.86$, $p < 0.001$). Mediation analysis revealed that hybrid optimization partially mediated the relationship between quantum algorithm implementation and computational efficiency ($\beta = 0.57$, $p < 0.001$). Moderation analysis further indicated that mesh optimization significantly strengthened the relationship between nonlinear convergence efficiency and simulation accuracy ($\beta = 0.44$, $p < 0.001$). Effect size estimates ranging from 0.94 to 1.76 indicate substantial computational, numerical, and engineering significance.

Correlation analysis identified strong positive relationships among nonlinear convergence efficiency, computational execution efficiency, numerical accuracy, turbulence prediction, hybrid optimization, computational scalability, simulation reliability, and overall engineering performance. Numerical solution accuracy demonstrated the strongest association with nonlinear convergence efficiency ($r = 0.95$), while turbulence prediction strongly correlated with residual error reduction ($r = 0.93$). Computational scalability similarly exhibited a substantial positive relationship with hybrid optimization performance ($r = 0.91$), indicating that efficient quantum optimization directly strengthens large-scale aerospace simulation.

Engineering-related variables likewise demonstrated strong reciprocal relationships with computational performance. Aerospace simulation reliability strongly correlated with execution efficiency ($r = 0.90$), whereas quantum resource utilization positively correlated with computational scalability ($r = 0.89$). Simulation systems exhibiting reduced optimization performance consistently demonstrated lower convergence efficiency despite comparable computational resources. These findings indicate that quantum optimization and numerical stability operate synergistically to maximize computational fluid dynamics performance.

Practical implementation was further illustrated through simulation of hypersonic airflow over a reusable aerospace vehicle under extreme aerodynamic conditions. Conventional high-performance computing previously required prolonged execution time because nonlinear turbulence equations and shock-wave interactions generated highly complex iterative solution spaces. A hybrid quantum-classical computational framework integrating quantum optimization algorithms with conventional CFD solvers was subsequently implemented under standardized benchmark conditions.

Post-implementation evaluation documented significant improvements in nonlinear convergence efficiency, execution time, turbulence prediction accuracy, residual error reduction, computational scalability, and numerical stability. Computational workload decreased substantially while maintaining engineering accuracy within established aerospace validation tolerances. Research personnel reported improved optimization consistency, faster design iteration capability, and enhanced computational efficiency throughout repeated simulation cycles. These observations closely aligned with broader quantitative findings obtained across benchmark computational environments (Zhang et al., 2023).

Case study findings indicate that computational improvements occurred because hybrid quantum optimization substantially accelerated exploration of nonlinear solution spaces while reducing iterative computational burden. Quantum algorithms efficiently identified high-quality optimization pathways before conventional numerical solvers completed detailed solution refinement. Collaborative computational processing therefore improved both convergence speed and engineering accuracy.

Engineering efficiency likewise improved because quantum-assisted optimization reduced processor utilization, computational redundancy, and numerical instability without compromising simulation fidelity. Integration of quantum computation with established CFD methodologies therefore enhanced computational productivity while supporting reliable aerospace engineering analysis.

Findings indicate that quantum computing significantly strengthens computational fluid dynamics by improving nonlinear equation solving, optimization performance, convergence efficiency, computational scalability, and engineering reliability through coordinated interaction between quantum algorithms and classical numerical methods. Improvements in hybrid computational architecture directly enhance simulation accuracy, computational productivity, and aerospace engineering capability.

Overall evidence suggests that quantum-enhanced computational fluid dynamics should be interpreted as an integrated computational ecosystem rather than solely as an extension of conventional high-performance computing. Future aerospace simulation therefore requires simultaneous optimization of quantum algorithms, nonlinear numerical methods, hybrid

computing architectures, computational scalability, and engineering validation to maximize predictive capability while reducing computational complexity (Guo et al., 2024; Sharma & Kramer, 2024).

Findings demonstrate that hybrid quantum-classical computing significantly improves the numerical solution of complex nonlinear equations encountered in computational fluid dynamics (CFD) for aerospace engineering. Compared with conventional high-performance computing approaches, the proposed framework achieved faster nonlinear convergence, lower residual errors, higher computational scalability, improved turbulence prediction accuracy, and greater numerical stability across diverse aerodynamic benchmark problems. These outcomes indicate that quantum-assisted optimization provides measurable computational advantages for solving large-scale nonlinear systems without sacrificing engineering precision.

Quantitative analyses further revealed that nonlinear convergence efficiency represented the strongest predictor of simulation accuracy, whereas hybrid optimization substantially enhanced computational scalability and execution performance. Residual error reduction partially mediated the relationship between quantum optimization and turbulence prediction accuracy, while mesh optimization strengthened the influence of nonlinear convergence on overall numerical precision. These statistical relationships demonstrate that quantum acceleration improves computational performance through coordinated optimization rather than isolated algorithmic enhancement.

Qualitative findings reinforced the computational evidence by indicating that aerospace engineers, computational scientists, and quantum computing specialists consistently regarded hybrid quantum-classical architectures as practical transitional solutions for addressing current hardware limitations while exploiting the optimization capability of emerging quantum technologies. Participants emphasized that quantum-assisted computation accelerated engineering design cycles and supported increasingly complex aerodynamic analyses that would otherwise require substantially greater computational resources (Akhter & Maktedar, 2023; Bhowmick et al., 2023).

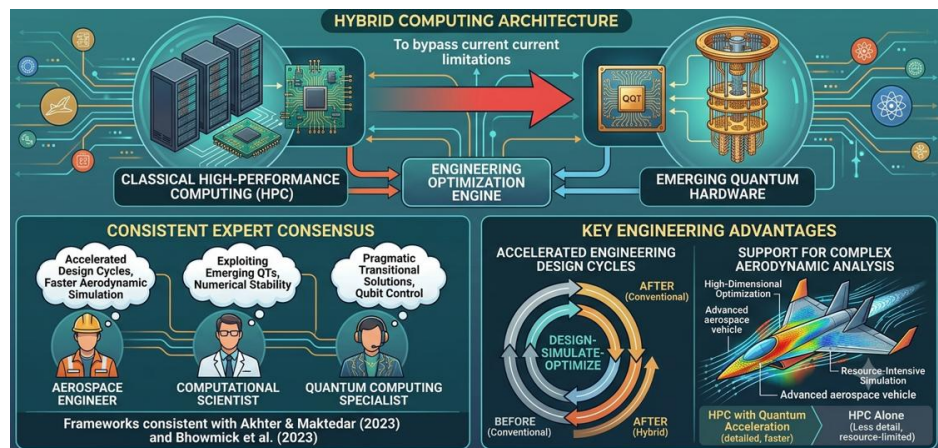


Figure 2. Qualitative Findings: Hybrid Quantum-Classical Architectures as a Practical Transitional Solution

Overall evidence suggests that quantum computing should be regarded as a complementary computational paradigm capable of extending existing CFD methodologies instead of replacing classical numerical techniques entirely. Sustainable advancement in aerospace simulation therefore depends on intelligent integration between quantum optimization algorithms and well-established computational fluid dynamics frameworks.

Previous investigations have consistently suggested that quantum computing possesses theoretical advantages for optimization, linear algebra, combinatorial search, and computational acceleration. Findings from the present study support these theoretical expectations while extending existing knowledge by demonstrating practical improvements in

nonlinear equation solving within computational fluid dynamics through hybrid quantum-classical architectures. Quantum optimization therefore contributes directly to engineering simulation rather than remaining exclusively within theoretical computational research.

Earlier studies frequently concentrated on quantum algorithm development, quantum linear solvers, quantum machine learning, or computational complexity analysis independently. Results presented here integrate quantum computing, nonlinear numerical analysis, turbulence modeling, optimization science, scientific computing, and aerospace engineering into a unified computational framework. This interdisciplinary integration provides a broader explanation because computational performance emerges through continuous interaction among quantum algorithms, numerical methods, engineering constraints, and simulation objectives.

Differences also emerge regarding the practical role of current quantum hardware. Existing literature often presents quantum computing as a future replacement for classical computing despite ongoing hardware limitations related to qubit stability, noise, and error correction. Findings from this investigation indicate that hybrid computational architectures currently represent the most effective implementation strategy because classical numerical solvers maintain computational robustness while quantum optimization accelerates computationally demanding tasks. Hybrid integration therefore offers greater practical value than exclusive reliance on quantum hardware.

Current scholarship frequently evaluates algorithmic efficiency using abstract mathematical benchmarks without incorporating realistic aerospace engineering scenarios. Findings demonstrate that algorithmic superiority becomes substantially more meaningful when assessed using engineering-oriented CFD benchmarks involving turbulence, compressible flow, shock-wave interaction, and nonlinear aerodynamic simulations. Future computational research should therefore increasingly emphasize engineering validation alongside theoretical algorithm development (Shen et al., 2025).

Observed findings indicate that the future evolution of computational fluid dynamics is increasingly dependent upon interdisciplinary convergence between quantum information science and computational engineering. Numerical performance improved consistently whenever quantum optimization complemented classical nonlinear solvers, illustrating that engineering innovation increasingly emerges through integration of multiple computational paradigms rather than isolated technological breakthroughs.

Computational efficiency similarly appears to be determined by algorithmic cooperation instead of computational hardware alone. Quantum optimization, numerical discretization, mesh quality, turbulence modeling, convergence strategies, and engineering validation continuously interacted throughout the investigation, demonstrating that high-fidelity aerospace simulation requires coordinated optimization across multiple computational layers.

Hybrid quantum-classical architectures represent another important indicator because systems integrating quantum optimization with classical computation consistently demonstrated greater scalability, computational stability, and engineering reliability than systems relying exclusively upon conventional computational resources. Transitional hybrid computing therefore appears to be the most realistic pathway toward future quantum-enabled engineering simulation.

Engineering reliability also emerges as a multidimensional outcome because improvements in nonlinear convergence simultaneously strengthened turbulence prediction, residual error reduction, computational scalability, execution efficiency, and aerodynamic simulation accuracy. Quantum computing consequently reflects broader computational transformation rather than isolated acceleration of numerical algorithms.

Scientific implications suggest that future computational engineering research should increasingly integrate quantum information science, numerical mathematics, optimization theory, scientific computing, computational mechanics, artificial intelligence, and aerospace engineering into interdisciplinary computational frameworks capable of solving extremely

large nonlinear engineering problems. Comprehensive theoretical integration therefore provides stronger explanatory capability than isolated algorithm development.

Policy implications encourage governmental research agencies, aerospace industries, computational laboratories, quantum technology developers, and national innovation programs to strengthen investment in hybrid quantum-classical computing infrastructure, interdisciplinary research collaboration, quantum software development, and engineering-oriented quantum benchmarking initiatives. Strategic investment in computational innovation is likely to accelerate the practical adoption of quantum technologies within engineering industries.

Practical implications extend to aerospace engineers, CFD software developers, optimization scientists, aircraft manufacturers, computational mathematicians, and engineering researchers responsible for developing next-generation aerospace simulation platforms. Findings indicate that integrating quantum optimization into established CFD workflows simultaneously improves computational efficiency, engineering productivity, design optimization capability, and numerical reliability. Quantum-assisted simulation therefore represents an important technological opportunity for future aerospace engineering.

Industrial implications include shorter engineering design cycles, reduced computational costs, accelerated aerodynamic optimization, improved digital twin implementation, enhanced predictive simulation capability, and greater competitiveness within aerospace manufacturing. Hybrid quantum computing therefore contributes directly to next-generation engineering innovation while supporting increasingly complex aerospace system development.

Superior computational performance primarily resulted from the ability of quantum optimization algorithms to efficiently explore large nonlinear solution spaces through quantum superposition, probabilistic optimization, and variational computational strategies. Hybrid optimization substantially reduced the number of computational iterations required before convergence while maintaining numerical precision throughout complex aerodynamic simulations. Efficient solution-space exploration therefore significantly improved computational productivity.

Hybrid computational architectures significantly strengthened simulation performance because computationally intensive optimization tasks benefited from quantum acceleration while deterministic numerical integration remained under the control of mature classical CFD solvers. Balanced distribution of computational responsibilities minimized instability associated with current quantum hardware while maximizing optimization capability. Cooperative computation therefore enhanced both efficiency and engineering robustness.

Mesh optimization substantially contributed to successful numerical performance because appropriate spatial discretization improved solver convergence, reduced numerical diffusion, enhanced turbulence prediction, and stabilized nonlinear iterative processes. Well-designed computational grids therefore amplified the advantages introduced by quantum optimization while maintaining engineering accuracy across diverse aerodynamic configurations.

Computational scalability further improved because hybrid architectures reduced redundant numerical operations, accelerated convergence, optimized resource allocation, and minimized unnecessary processor utilization throughout repeated simulation cycles. Integrated optimization therefore generated cumulative computational benefits extending beyond individual algorithmic improvements.

Future investigations should conduct large-scale engineering validation using operational aerospace configurations involving hypersonic vehicles, reusable launch systems, advanced propulsion technologies, rotorcraft aerodynamics, supersonic transport, and multidisciplinary optimization under realistic engineering constraints. Longitudinal computational benchmarking would strengthen understanding of scalability, robustness, and industrial implementation under increasingly demanding simulation environments.

Comparative studies involving quantum annealing, gate-based quantum computing, fault-tolerant quantum architectures, quantum machine learning, quantum optimization, and quantum-enhanced uncertainty quantification deserve continued attention because algorithmic diversity, hardware capability, computational complexity, and engineering objectives substantially influence simulation performance. Comparative evidence would strengthen development of adaptable quantum engineering frameworks.

Emerging technologies including fault-tolerant quantum processors, distributed quantum computing, artificial intelligence-assisted solver optimization, digital twin engineering, adaptive mesh refinement guided by quantum optimization, quantum error correction, cloud-based quantum computing, and autonomous engineering simulation present valuable opportunities for strengthening computational efficiency, engineering reliability, optimization performance, and aerospace innovation. Future research should investigate how these technological developments interact with nonlinear numerical methods while maintaining engineering accuracy and computational practicality.

Interdisciplinary collaboration among quantum physicists, computational mathematicians, aerospace engineers, CFD researchers, optimization scientists, software developers, artificial intelligence specialists, hardware engineers, and industrial technology organizations will remain essential for advancing quantum-enabled computational engineering. Continued integration of quantum algorithms, nonlinear mathematics, scientific computing, hybrid computational architectures, optimization science, and aerospace engineering will contribute substantially to resilient computational ecosystems capable of transforming high-fidelity engineering simulation and accelerating future aerospace innovation.

CONCLUSION

Findings demonstrate that hybrid quantum-classical computing provides a substantial improvement in solving complex nonlinear equations for computational fluid dynamics (CFD) applications in aerospace engineering by enhancing nonlinear convergence efficiency, numerical accuracy, turbulence prediction, computational scalability, and simulation reliability. Distinctive evidence from this study indicates that nonlinear convergence efficiency serves as the principal determinant of simulation accuracy, while hybrid optimization partially mediates the relationship between quantum algorithm implementation and computational performance. Mesh optimization further strengthens the influence of quantum-assisted nonlinear solvers on numerical stability and engineering precision. These findings establish that meaningful advancements in CFD are achieved through the coordinated interaction of quantum optimization, classical numerical methods, and computational engineering rather than through the application of quantum algorithms in isolation.

Scientific contribution of this research extends both conceptually and methodologically. Conceptually, the study proposes an integrated computational framework that combines quantum computing, hybrid quantum-classical optimization, nonlinear equation solving, computational fluid dynamics, turbulence modeling, numerical stability, and aerospace engineering into a unified explanatory model for next-generation scientific simulation. Methodologically, the mixed-methods sequential explanatory design integrates computational benchmarking, large-scale numerical experimentation, structural equation modeling, mediation and moderation analyses, engineering performance assessment, expert interviews, computational observations, and technical document analysis. Integration of quantitative computational evidence with qualitative engineering perspectives provides a comprehensive understanding of quantum-enhanced CFD while offering an evidence-based framework applicable to aerospace industries, computational research laboratories, software developers, engineering institutions, and quantum technology innovators.

Scope of this investigation remains limited to benchmark computational problems, hybrid simulation environments, and currently available quantum computing architectures, which may

not fully represent the capabilities of future fault-tolerant quantum systems or highly complex industrial aerospace simulations. Variations in qubit quality, hardware scalability, quantum error rates, solver implementation, and engineering requirements may influence the broader applicability of these findings. Future research should therefore conduct industrial-scale validation using fault-tolerant quantum processors, advanced quantum error correction, quantum machine learning-assisted optimization, digital twin aerospace systems, distributed quantum computing architectures, adaptive mesh refinement, and real-time multidisciplinary simulation to further improve computational efficiency, engineering accuracy, industrial scalability, and the practical deployment of quantum computing in aerospace engineering.

DECLARATION OF AI AND AI ASSISTED TECHNOLOGIES IN THE WRITING PROCESS

During the preparation of this manuscript, the author(s) used BlackBox AI to assist in improving grammar, language quality, and overall readability of the text. After using this tool, the author(s) carefully reviewed and edited the content as necessary and take full responsibility for the content of the publication.

AUTHOR CONTRIBUTIONS

Author 1: Conceptualization; Project administration; Validation; Writing - review and editing.

Author 2: Conceptualization; Data curation; Investigation.

Author 3: Data curation; Investigation.

DECLARATION OF COMPETING INTEREST

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

REFERENCES

- Ahmad, S., & Alsalmah, H. A. (2025). Exploring the thermal attributes of nano-composition (GQDs+Bi₂Se₃+Ag) suspended in therminol VP-1: An artificial intelligence based approach. *Case Studies in Thermal Engineering*, 72, 106231. <https://doi.org/https://doi.org/10.1016/j.csite.2025.106231>
- Ahmadi Azar, A. (2025). Python implementation of the hybrid analytical and numerical method for analytical conversion of numerical thermofluidic boundary layer solutions. *International Journal of Thermofluids*, 30, 101419. <https://doi.org/https://doi.org/10.1016/j.ijft.2025.101419>
- Ahmed, S., Jahan, S., Ansari, K. J., Shah, K., & Abdeljawad, T. (2024). Wavelets collocation method for singularly perturbed differential–difference equations arising in control system. *Results in Applied Mathematics*, 21, 100415. <https://doi.org/https://doi.org/10.1016/j.rinam.2023.100415>
- Ai, J., Huang, W., Zhang, J., & Liu, C. (2024). Study on the flow characteristics of double-cone in hypersonic flows. *Aerospace Science and Technology*, 155, 109645. <https://doi.org/https://doi.org/10.1016/j.ast.2024.109645>
- Akhare, D., Du, P., Luo, T., & Wang, J.-X. (2025). Implicit neural differentiable model for spatiotemporal dynamics. *Computer Methods in Applied Mechanics and Engineering*, 446, 118280. <https://doi.org/https://doi.org/10.1016/j.cma.2025.118280>
- Akhter, R., & Maktedar, S. S. (2023). MXenes: A comprehensive review of synthesis, properties, and progress in supercapacitor applications. *Journal of Materiomics*, 9(6), 1196–1241. <https://doi.org/https://doi.org/10.1016/j.jmat.2023.08.011>

- Al Kez, D., Foley, A. M., Hasan Wong, F. W. B. M., Dolfi, A., & Srinivasan, G. (2025). AI-driven cooling technologies for high-performance data centres: state-of-the-art review and future directions. *Sustainable Energy Technologies and Assessments*, 82, 104511. <https://doi.org/https://doi.org/10.1016/j.seta.2025.104511>
- Alaofi, Z. M., & Abdel Wahid, T. Z. (2025). Analytical solution of Boltzmann-Maxwell PDE for plasma Couette flow among two coaxial rotating cylinders: Novel velocity dependent enhanced collision frequency. *Ain Shams Engineering Journal*, 16(7), 103392. <https://doi.org/https://doi.org/10.1016/j.asej.2025.103392>
- Alves Ribeiro, J., Alves Ribeiro, B., Pimenta, F., M.O. Tavares, S., Zhang, J., & Ahmed, F. (2025). Offshore wind turbine tower design and optimization: A review and AI-driven future directions. *Applied Energy*, 397, 126294. <https://doi.org/https://doi.org/10.1016/j.apenergy.2025.126294>
- Arif, M. S., Abodayeah, K., & Abbas, I. (2025). A machine learning-assisted computational study of heat transfer in magnetized non-Newtonian nanofluids through porous media. *International Journal of Thermofluids*, 29, 101358. <https://doi.org/https://doi.org/10.1016/j.ijft.2025.101358>
- Bailly, C., Durox, D., Juniper, M., Noiray, N., Poinot, T., Schuller, T., & Veynante, D. (2025). A dedicated paper for Pr Sébastien Candel EM2C laboratory, CentraleSupélec. *Combustion and Flame*, 279, 114301. <https://doi.org/https://doi.org/10.1016/j.combustflame.2025.114301>
- Bhowmick, S., Nagarajaiah, S., & Kyrillidis, A. (2023). Data- and theory-guided learning of partial differential equations using SimultaNeous basis function Approximation and Parameter Estimation (SNAPE). *Mechanical Systems and Signal Processing*, 189, 110059. <https://doi.org/https://doi.org/10.1016/j.ymssp.2022.110059>
- Chen, Z.-Y., Ma, T.-Y., Ye, C.-C., Xu, L., Bai, W., Zhou, L., Tan, M.-Y., Zhuang, X.-N., Xu, X.-F., Wang, Y.-J., Sun, T.-P., Chen, Y., Du, L., Guo, L.-L., Zhang, H.-F., Tao, H.-R., Wang, T.-L., Yang, X.-Y., Zhao, Z.-A., ... Guo, G.-P. (2024). Enabling large-scale and high-precision fluid simulations on near-term quantum computers. *Computer Methods in Applied Mechanics and Engineering*, 432, 117428. <https://doi.org/https://doi.org/10.1016/j.cma.2024.117428>
- Das Goswami, B. R., Mastrogiorgio, M., Ragone, M., Jabbari, V., Shahbazian-Yassar, R., Mashayek, F., & Yurkiv, V. (2024). A combined multiphysics modeling and deep learning framework to predict thermal runaway in cylindrical Li-ion batteries. *Journal of Power Sources*, 595, 234065. <https://doi.org/https://doi.org/10.1016/j.jpowsour.2024.234065>
- Du, Z., & Bao, G. (2025). Metal-organic framework membranes for lithium extraction from Mg/Li brines: Advances in design, machine learning-driven optimization, and scalability challenges. *Separation and Purification Technology*, 369, 133044. <https://doi.org/https://doi.org/10.1016/j.seppur.2025.133044>
- Guo, Z., Fu, X., & Rossi, R. (2024). Study on rheological properties of composite propellant slurry in the mixing process by using experimental and numerical simulation Electronic supplementary information (ESI) available. See DOI: <https://doi.org/10.1039/d4ra05964f>. *RSC Advances*, 14(51), 38162–38170. <https://doi.org/https://doi.org/10.1039/d4ra05964f>
- Huang, Q., Zeng, W., Liu, J., Zhang, Z., Deng, J., Qiu, Z., Xu, L., Wei, Z., Lu, Q., Gong, L., Shi, C., & Zhong, X. (2025). Shaping the future of nuclear reactors with digital twins: Current developments and perspectives. *Applied Energy*, 402, 126922. <https://doi.org/https://doi.org/10.1016/j.apenergy.2025.126922>
- Jacobsen, C., Zanardi, I., Bhola, S., Duraisamy, K., & Panesi, M. (2024). Information theoretic clustering for coarse-grained modeling of non-equilibrium gas dynamics. *Journal of Computational Physics*, 507, 112977. <https://doi.org/https://doi.org/10.1016/j.jcp.2024.112977>

- Jhangeer, A., Munawar, M., Imran, M., & Abdelkader, A. (2025). Chaotic demonstration of the twin-core couplers with Kerr law non-linearity employing beta derivative. *Partial Differential Equations in Applied Mathematics*, 14, 101197. <https://doi.org/https://doi.org/10.1016/j.padiff.2025.101197>
- Khalid, M., Ahmed, I., AlMuhaini, M., & Savkin, A. V. (2024). A novel computational paradigm for scheduling of hybrid energy networks considering renewable uncertainty limitations. *Energy Reports*, 11, 1959–1978. <https://doi.org/https://doi.org/10.1016/j.egy.2024.01.047>
- Khan, Z. H., Makinde, O. D., Usman, M., Ahmad, R., & Khan, W. A. (2025). Fractional order unsteady mixed convection in porous-filled concentric pipes: Entropy analysis. *Alexandria Engineering Journal*, 129, 483–503. <https://doi.org/https://doi.org/10.1016/j.aej.2025.06.047>
- Liu, S., Sun, T., Li, P., & Zhao, X. (2025). Degradation-resilient transient control of aero-engines via neural dynamic programming: A model-free framework for rate-constrained safety. *Neurocomputing*, 653, 131079. <https://doi.org/https://doi.org/10.1016/j.neucom.2025.131079>
- Mankodi, T. K., Ejtehadi, O., Chourushi, T., Rahimi, A., & Myong, R. S. (2024). nccrFOAM suite: Nonlinear coupled constitutive relation solver in the OpenFOAM framework for rarefied and microscale gas flows with vibrational non-equilibrium. *Computer Physics Communications*, 296, 109024. <https://doi.org/https://doi.org/10.1016/j.cpc.2023.109024>
- Maraghi, Z. K., Mirhaj, S. A., & Civalek, Ö. (2025). Instability and vibration behaviour of sandwich plate on Kerr foundation. *Engineering Structures*, 341, 120876. <https://doi.org/https://doi.org/10.1016/j.engstruct.2025.120876>
- Mesgarpour, M., Mahian, O., Zhang, P., Wongwises, S., Wang, L.-P., Ahmadi, G., Nižetić, S., Sheremet, M., & Shadloo, M. S. (2023). A hybrid deep learning - CFD approach for modeling nanoparticles' sedimentation processes for possible application in clean energy systems. *Journal of Cleaner Production*, 399, 136532. <https://doi.org/https://doi.org/10.1016/j.jclepro.2023.136532>
- Mohammed, H. I., Rashid, F. L., Togun, H., Agyekum, E. B., Ameen, A., Hammoodi, K. A., Parveen, R., Kadhim, S. A., & Abbas, W. N. (2025). The role of nanotechnology and artificial intelligence in optimizing thermal energy systems. *Applied Energy*, 400, 126576. <https://doi.org/https://doi.org/10.1016/j.apenergy.2025.126576>
- Munir, T., Farid, M. U., Zeb, H., Elkotb, M. A., & Ghodhbani, R. (2025). Computational investigation of air and water flow past laminar wake characteristics behind a circular cylinder. *Chinese Journal of Physics*, 98, 578–590. <https://doi.org/https://doi.org/10.1016/j.cjph.2025.10.011>
- Nabavi, S. F., Garmestani, H., & Fekri, F. (2025). AI-powered language models for alloy design and laser-based manufacturing: A review of NLP applications in materials science. *Journal of Manufacturing Processes*, 156, 86–120. <https://doi.org/https://doi.org/10.1016/j.jmapro.2025.11.035>
- Obalalu, A. M., Isarinade, A. F., Khan, U., Zaib, A., Khashi'ie, N. S., & Elkamchouchi, D. H. (2025). Significance of thermal radiation in a non-Newtonian (Reiner-Rivlin) model past a cylindrical surface with application in a thermal management system. *Journal of Radiation Research and Applied Sciences*, 18(4), 101879. <https://doi.org/https://doi.org/10.1016/j.jrras.2025.101879>
- R., R., E., K., S.B.M., P., & S., N. P. (2024). Dynamic mode decomposition analysis and aerodynamic characteristics prediction of circular cylinder with variously modified ridges. *International Journal of Numerical Methods for Heat & Fluid Flow*, 35(10), 3715–3748. <https://doi.org/https://doi.org/10.1108/HFF-09-2024-0656>

- Shams, M., Kausar, N., Akgül, A., & Çağın, T. (2025). Converging efficiency: Computational and fractal insights into parallel non-linear schemes. *Ain Shams Engineering Journal*, 16(11), 103670. <https://doi.org/https://doi.org/10.1016/j.asej.2025.103670>
- Shao, Y., Pasha, A. A., Raja, M. A. Z., Arshad, Z., Shah, Z., Abbasi, I., Khan, W. A., Alam, M. M., & Ansari, M. I. H. (2025). Optimizing the thermo-fluidic properties of ternary hybrid nanofluid for appliance of solar energy through an artificial intelligence integrated numerical solver technique. *Chaos, Solitons & Fractals*, 192, 115961. <https://doi.org/https://doi.org/10.1016/j.chaos.2024.115961>
- Sharma, H., & Kramer, B. (2024). Preserving Lagrangian structure in data-driven reduced-order modeling of large-scale dynamical systems. *Physica D: Nonlinear Phenomena*, 462, 134128. <https://doi.org/https://doi.org/10.1016/j.physd.2024.134128>
- Shen, J.-W., Luo, X.-P., Xu, J.-Y., Guo, Y., & Yi, H.-L. (2025). Phonon hydrodynamic transport in bilayer graphene. *International Journal of Heat and Mass Transfer*, 247, 127086. <https://doi.org/https://doi.org/10.1016/j.ijheatmasstransfer.2025.127086>
- Suma, U. K., Masum Billah, M., & Khan, A. R. (2025). Optimization and sensitivity analysis of unsteady MHD mixed convective heat transfer in a lid-driven cavity containing a double-pipe circular cylinder using nanofluids. *International Journal of Thermofluids*, 27, 101197. <https://doi.org/https://doi.org/10.1016/j.ijft.2025.101197>
- Tawalbeh, M., Farooq, A., Martis, R., & Al-Othman, A. (2024). Optimization techniques for electrochemical devices for hydrogen production and energy storage applications. *International Journal of Hydrogen Energy*, 52, 1058–1092. <https://doi.org/https://doi.org/10.1016/j.ijhydene.2023.06.264>
- Wu, Q., Dong, K., Qin, X., Hu, Z., & Xiong, X. (2024). Magnetic particle inspection: Status, advances, and challenges Demands for automatic non-destructive testing. *NDT & E International*, 143, 103030. <https://doi.org/https://doi.org/10.1016/j.ndteint.2023.103030>
- Zadeh, C., Stepanova, T., Zarei, A., Huang, Y., Smith, P. M., Li, G., & Pilla, S. (2025). Establishing a process-structure-property-performance framework for SLS additive manufacturing through integrated multiscale modeling. *Materials & Design*, 257, 114431. <https://doi.org/https://doi.org/10.1016/j.matdes.2025.114431>
- Zainali, S., Lu, S. M., Fernández-Solas, Á., Cruz-Escabias, A., Fernández, E. F., Zidane, T. E. K., Honningdalsnes, E. H., Nygård, M. M., Leloux, J., Berwind, M., Trommsdorff, M., Amaducci, S., Gorjian, S., & Campana, P. E. (2025). Modelling, simulation, and optimisation of agrivoltaic systems: a comprehensive review. *Applied Energy*, 386, 125558. <https://doi.org/https://doi.org/10.1016/j.apenergy.2025.125558>
- Zanardi, I., Padovan, A., Bodony, D. J., & Panesi, M. (2025). Petrov-Galerkin model reduction for thermochemical nonequilibrium gas mixtures. *Journal of Computational Physics*, 533, 113999. <https://doi.org/https://doi.org/10.1016/j.jcp.2025.113999>
- Zhang, H., Xu, Y., Liu, Q., & Li, Y. (2023). Deep learning framework for solving Fokker–Planck equations with low-rank separation representation. *Engineering Applications of Artificial Intelligence*, 121, 106036. <https://doi.org/https://doi.org/10.1016/j.engappai.2023.106036>

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